

Quarter 1

Quarter 1	Quarter 2		Quarter 3		Quarter 4	
Various Functions & Their Graphs, Polynomials & Polynomial Functions, Inverse Functions	Trigonometric Functions and Their Graphs, Unit Circle, Inverse Trigonometric Functions, Law of Sines, Law of Cosines, Trigonometric Identities		Exponential and Logarithmic Functions, Conic Sections		Systems of Equations and Matrices, Polar Coordinates and Complex Numbers, Sequences and Series, Limits and Introduction to Integrals	
August 12, 2019 – October 11, 2019	October 21, 2019 – December 20, 2019		January 6, 2020 – March 13, 2020		March 23, 2020 – May 22, 2020	
P.F.IF.A.1	P. G.AT.A.1	P.F.GT.A.8	P.A.PE.A.1	P.N.NE.A.2	P. A. REI.A.1	P.A.S.A.1
P.F.IF.A.2	P.G.AT.A.3	P.G.TI.A.2	P.A.PE.A.2		P. A. REI.A.2	P.A.S.A.2
P.F.IF.A.4	P.G.AT.A.5		P. A.C.A.2		P. N. VM.A.1	P.A.S.A.3
P.F.IF.A.5	P.G.AT.A.6		P. A.C.A.3		P. N. VM.A.2	P.A.S.A.4
P.F.IF.A.6	P.F.TF.A.1		P.F.IF.A.2		P. N. VM.A.3	P.A.S.A.5
P.F.IF.A.7	P.F.TF.A.2		P.F.IF.A.3		P. N. VM.B.4	P. N. VM.C.13
P.F.BF.A.1	P.F.GT.A.3		P.F.IF.A.5		P. N. VM.B.5	Calculus C.F.LF.A.2
P.F.BF.A.3	P.F.GT.A.4		P.S.MD.A.1		P. N. VM.B.6	Calculus C.F.UI.A.3
P.F.BF.A.5	P.F.GT.A.5		P.S.MD.A.2		P.G.PC.A.1	
P.F.BF.A.6	P.F.GT.A.6		P.S.MD.A.3		P.G.PC.A.2	
P.N.CN.B.7	P.F.GT.A.7		P.N.NE.A.1		P.G.PC.A.3	



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Precalculus

Introduction

Destination 2025, Shelby County Schools' 10-year strategic plan, is designed not only to improve the quality of public education, but also to create a more knowledgeable, productive workforce and ultimately benefit our entire community.

What will success look like?



In order to achieve these ambitious goals, we must collectively work to provide our students with high quality, college and career ready aligned instruction. The Tennessee State Standards provide a common set of expectations for what students will know and be able to do at the end of a grade. The State of Tennessee provides two sets of standards, which include the Standards for Mathematical Content and The Standards for Mathematical Practice. The Content Standards set high expectations for all students to ensure that Tennessee graduates are prepared to meet the rigorous demands of mathematical understanding for college and career. The eight Standards for Mathematical Practice describe the varieties of expertise, habits of mind, and productive dispositions that educators seek to develop in all students. The Tennessee State Standards also represent three fundamental shifts in mathematics instruction: focus, coherence and rigor.

Instructional Shifts for Mathematics



Throughout this curriculum map, you will see resources as well as links to tasks that will support you in ensuring that students are able to reach the demands of the standards in your classroom. In addition to the resources embedded in the map, there are some high-leverage resources around the content standards and mathematical practice standards that teachers should consistently access. For a full description of each, click on the links below.



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How to Use the Maps

Overview

An overview is provided for each quarter and includes the topics, focus standards, intended rigor of the standards and foundational skills needed for success of those standards.

Your curriculum map contains four columns that each highlight specific instructional components. Use the details below as a guide for information included in each column.

Tennessee State Standards

TN State Standards are located in the left column. Each content standard is identified as Major Content or Supporting Content (for Algebra I, Algebra II & Geometry only). A key can be found at the bottom of the map.

Content

This section contains learning objectives based upon the TN State Standards. Best practices tell us that clearly communicating measurable objectives lead to greater student understanding. Additionally, essential questions are provided to guide student exploration and inquiry.

Instructional Support & Resources

District and web-based resources have been provided in the Instructional Support & Resources columns. You will find a variety of instructional resources that align with the content standards. The additional resources provided should be used as needed for content support and scaffolding. The inclusion of vocabulary serves as a resource for teacher planning and for building a common language across K-12 mathematics. One of the goals for Tennessee State Standards is to create a common language, and the expectation is that teachers will embed this language throughout their daily lessons.

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Topics Addressed in Quarter

- Various Functions & Their Graphs
- Polynomials & Polynomial Functions
- Inverse Functions

Overview

In this quarter students develop conceptual knowledge of functions that set the stage for the learning of other standards in Precalculus. Students apply the standards in Interpreting Functions and Building Functions in the cases of polynomial functions of degree greater than two, more complicated rational functions, the reciprocal trigonometric functions, and inverse trigonometric functions. Students will examine end behavior of functions and learn how to find asymptotes. Students further their understanding of inverse functions and construct inverse functions by appropriately restricting domains.

TN STATE STANDARDS CONTENT		INSTRUCTIONAL SUPPORT & RESOURCES	
GLENCOE - Chapter 1: Functions from a Calculus Perspective			
50	JLLIVAN – Chapter 2: Functions & Their Graphs	Chapter 5: Exponential & Logarithmic Funct	lions
	(Allow approximately 6 weeks for in	nstruction, review, and assessment)	
Domain: Interpreting Functions	Essential Question(s):	Glencoe	Vocabulary: set-builder notation, interval
Cluster: Analyze functions using different	 How can functions describe real-world 	1-1: Functions	notation, implied domain, piecewise-defined
representations.	situations, model predictions and solve	1-2: Analyzing Graphs of Functions and	function, relevant domain, continuous, limit
<u>P.F.IF.A.1</u> Determine whether a function is	problems?	Relations	discontinuous, infinite, jump, point, removable
even, odd, or neither.	How can you use the number of sign	1-3: Continuity, End Behavior, and Limits	and non-removable discontinuities, end
P.F.IF.A.2 Analyze qualities of exponential,	changes in a function to determine the	Sullivan	behavior
polynomial, logarithmic, trigonometric, and	number and type of real zeros of a function?	2.1: Functions	
rational functions and solve real world		2.2: The Graph of a Function	Writing in Math:
problems that can be modeled with these	Objective(s):	2.3: Properties of Functions	 Write two things you already know about
functions (by hand and with appropriate	Students will:		functions.
technology). ★	 Identify and evaluate functions and 	Tasks:	
P.F.IF.A.4 Identify the real zeros of a function	state their domains in symbolic and	Illustrative Math: Identifying Even and Odd	• Give an example of a real-life situation that is
and explain the relationship between the real	verbal forms.	Functions	a function, and explain the type of function
zeros and the x-intercepts of the graph of a	Use graphs of functions to estimate		(linear, quadratic) it is. Explain whether and
function (exponential, polynomial, logarithmic,	function values and find domains.		how the domain and range of the function are
trigonometric, and rational).	ranges, y-intercepts, and zeros of		restricted, given the situation. Explain what



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TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUPPORT & RESOURCES	
<u>P.F.IF.A.5</u> Identify characteristics of graphs based on a set of conditions or on a general equation such as $y = ax^2 + c$. <u>P.F.IF.A.7</u> Graph rational functions, identifying zeros, asymptotes (including slant), and holes (when suitable factorizations are available) and showing end-behavior.	 functions. Determine symmetry of graphs and identify even and odd functions. Determine intervals on which a function is continuous. Describe end behavior of functions. 	Additional Resources: <u>Function Notation: Even and Odd</u> <u>Khan Academy: Recognizing Even and Odd</u> <u>Functions</u> <u>Functions and Graphs Videos</u>	the x-intercept and the <i>y</i> -intercept represent in the situation.
Domain: Interpreting Functions Cluster: Analyze functions using different representations. <u>P.F.IF.A.6</u> Visually locate critical points on the graphs of functions and determine if each critical point is a minimum, a maximum, or point of inflection. Describe intervals where the function is increasing or decreasing and where different types of concavity occur.	 Essential Question(s): How can we use the definite integral in real- world applications? Objective(s): Students will: Determine intervals on which functions are increasing, constant, or decreasing, concave up or concave down, maxima, minima, and points of inflection. 	Glencoe 1-4: Extrema and Average Rates of Change Sullivan 2.3: Properties of Functions Task(s): Inside Math: Quadratics Performance Task Additional Resources: Engage NY: End Behavior of Rational Functions Curve Sketching Tutorial Functions and Graphs Videos	 Vocabulary: increasing, decreasing, constant, maximum, minimum, extrema, average rate of change, secant line Writing in Math: Describe how the average rate of change of a function relates to a function when it is increasing, decreasing, and constant on an interval.
Domain: Building Functions Cluster: Build new functions from existing functions. <u>P.F.BF.A.1</u> : Understand how the algebraic properties of an equation transform the geometric properties of its graph. For example, given a function, describe the transformation of the graph resulting from the manipulation of the algebraic properties of the equation (i.e., translations, stretches, reflections and changes in periodicity and amplitude).	 Essential Question(s): How can changing the values of a function affect the shape of the graph of the function? Objective(s): Students will: Identify, describe, and graph transformations of parent functions. 	Glencoe 1-5: Parent Functions and Transformations Sullivan 2.4: Library of Functions 2.5: Graphing Techniques: Transformations Additional Resource(s): Functions and Graphs Videos	 Vocabulary: parent function, constant function, zero function, identity function, quadratic function, cubic function, square root function, reciprocal function, absolute value function, step function, greatest integer function, transformation, translation, reflections, dilation Writing in Math: Use words, graphs, tables and equations to relate parent functions and transformations. Show this relationship through a specific example.



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TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUPPORT & RESOURCES	
Domain: Building Functions Cluster: Build new functions from existing functions. P.F.IF.A.2 : Develop an understanding of functions as elements that can be operated upon to get new functions: addition, subtraction, multiplication, division, and composition of functions. P.F.BF.A.3 Compose functions. For example, <i>if</i> $T(y)$ <i>is the temperature in the atmosphere as</i> <i>a function of height, and</i> $h(t)$ <i>is the height of a</i> <i>weather balloon as a function of time, then</i> T(h(t)) <i>is the temperature at the location of the</i> <i>weather balloon as a function of time.</i>	 Essential Question(s): What relationships exist between quantities that can be modeled by functions? Objective(s): Students will: Perform arithmetic operations with functions. Compose compositions of functions. 	Glencoe 1-6: Function Operations and Composition of Functions Sullivan 5-1: Composite Functions Task(s): Illustrative Math: Compose Functions Additional Resources: Engage NY Lesson 16: Function Composition Engage NY Lesson 17: Solving Problems by Function Composite Functions Applications TI Nspire Composite Functions Activity How to Add, Subtract, Multiply and Divide Functions Functions and Graphs Videos	Vocabulary: compose, composite function Writing in Math: Explain how to determine the output of a composition of functions, given the input.
 Domain: Building Functions Cluster: Build new functions from existing functions. P.F.BF.A.5 Find inverse functions (including exponential, logarithmic and trigonometric). a. Calculate the inverse of a function, <i>f</i> (<i>x</i>), with respect to each of the functional operations; in other words, the additive inverse, -<i>f</i>(<i>x</i>), the multiplicative inverse, 1/f(x), and the inverse with respect to composition, <i>f</i>⁻¹(<i>x</i>). Understand the algebraic and graphical implications of each type. b. Verify by composition that one 	 Essential Question(s): What are inverse functions and what are they being used for? How do we restrict the domain of a non-invertible function to produce an invertible function? Objective(s): Students will: Use the horizontal line test to determine whether a function has an inverse function. Find inverse functions algebraically and graphically. Verify inverse functions algebraically using a composition of functions and graphically using y=x symmetry. 	Glencoe 1-7: Inverse Relations and Functions Sullivan 5.2: One-to-One Functions; Inverse Functions Task(s): Illustrative Math: Invertible or Not Graphs of Compositions Additional Resources: Engage NY Lessons: Inverse Functions (Lessons 18-21) Inverse Functions Concept Development Activity Functions and Graphs Videos	 Vocabulary: inverse function, one-to-one, invertible Writing in Math: Explain what it means for a function to be "one-to-one" and describe two methods for determining whether or not a function is one-to-one. Justify the identity function, y= x, being the line of reflection for a function and its inverse.



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TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUPPORT & RESOURCES	
 function is the inverse of another. c. Read values of an inverse function from a graph or a table, given that the function has an inverse. d. Recognize a function is invertible if and only if it is one-to-one. Produce an inverse is function with a function on a second second			
an invertible function from a non- invertible function by restricting the domain. P.F.BF.A.6 : Explain why the graph of a function and its inverse are reflections of one another over the line y=x.			
·	GLENCOE - Chapter 2: Power, P	olvnomial. & Rational Functions	
	SULLIVAN – Chapter 4: Poly	nomial & Rational Functions	
	(Allow approximately 3 weeks for in	nstruction, review, and assessment)	
Domain: Interpreting Functions Cluster: Analyze functions using different representations. P.F.IF.A.2: Analyze qualities of exponential, polynomial, logarithmic, trigonometric, and rational functions and solve real world problems that can be modeled with these functions (by hand and with appropriate technology). ★	 Essential Question(s): What relationships exist between quantities that can be modeled by functions? What are some of the characteristics of the graph of an exponential function? What are some of the characteristics of the graph of a logarithmic function? Objective(s): Students will: Graph and analyze power functions and radical functions. Graph polynomial functions. Model real-world data with polynomial functions. 	Glencoe 2-1: Power and Radical Functions 2-2: Polynomial Functions Sullivan 4.1: Polynomial Functions and Models Task(s): Writing an Exponential Function from a Description Illustrative Math: Model with Exponential Functions Exponential and Logarithmic Functions (tasks start on p. 12) Additional Resources:	 Vocabulary: power function, monomial function, extraneous solutions, polynomial function, polynomial function of degree n, leading coefficient, leading term test, quartic function, turning points, quadratic form, repeated zero, multiplicity Writing in Math: Describe some similarities and differences between the graphs of exponential, polynomial, logarithmic, trigonometric, and rational functions.



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TN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUPPORT & RESOURCES		
Domain: Interpreting Functions Cluster: Analyze functions using different	Essential Question(s): How do polynomial functions model real- 	Analyzing-the-Graph-of-a-Rational-Function- Asymptotes-Domain-and-Range Polynomial and Rational Functions Videos Glencoe 2-3: The Remainder and Factor Theorems	Vocabulary: synthetic division, depressed polynomial, synthetic substitution, rational	
representations. <u>P.F.IF.A.4</u> : Identify the real zeros of a function and explain the relationship between the real zeros and the x-intercepts of the graph of a function (exponential, polynomial, logarithmic, trigonometric, and rational).	 world problems and their solutions? Why are complex numbers necessary? Objective(s): Students will: Find the real zeroe of polynomial 	 2-4: Zeros of Polynomial Functions Sullivan 4.5: The Real Zeros of a Polynomial Function 4.6: Complex Zeros; Fundamental Theorem of Algebra 	zero theorem, lower bound, upper bound, Decartes' Rule of Signs, Fundamental Theorem of Algebra, Linear Factorization Theorem, Conjugate Root Theorem, complex conjugate, irreducible over the reals Writing in Math:	
Domain: Complex numbers Cluster: Use complex numbers in polynomial identities and equations. <u>P.N.CN.B.7</u> Know the Fundamental Theorem of Algebra; show that it is true for quadratic polynomials.	 Find the real zeros of polynomial functions. Find the complex zeros of polynomial functions and know and use the Fundamental Theorem of Algebra. 	Task(s): Illustrative Math: Zeroes and Factorization of General Polynomials Factors, Zeroes, and Roots: Oh My! (Teacher notes p. 27 and student pages start on p. 39) Additional Resources: Khan Academy: Fundamental Theorem of Algebra Khan Academy: Zeroes or Polynomials and Their Graphs Polynomial and Rational Functions Videos	Explain how you can use a graphing calculator, synthetic division and factoring to completely factor a fifth-degree polynomial with rational coefficients, three integral zeroes and two non-integral, rational zeroes.	
Domain : Interpreting Functions Cluster: Analyze functions using different representations.	 Essential Questions(s): What relationships exist between quantities that can be modeled by functions? 	Glencoe 2-5: Rational Functions Sullivan 4.2: Properties of Rational Functions	Vocabulary: rational function, asymptote, horizontal asymptote, vertical asymptote, oblique asymptote, holes	
P.F.IF.A.2 Analyze qualities of exponential, polynomial, logarithmic, trigonometric, and rational functions and solve real world problems that can be modeled with these	Objective(s):Students will:Analyze and graph rational functions,	4.3: The Graph of a Rational Function Task(s):	Writing in Math:	



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IN STATE STANDARDS	CONTENT	INSTRUCTIONAL SUPPORT & RESOURCES	
functions (by hand and with appropriate technology). ★ P.F.IF.A.4 Identify the real zeros of a function and explain the relationship between the real zeros and the x-intercepts of the graph of a function (exponential, polynomial, logarithmic, trigonometric, and rational). P.F.IF.A.7 Graph rational functions, identifying zeros, asymptotes (including slant), and holes (when suitable factorizations are available) and showing end-behavior.	 including horizontal, vertical, and oblique asymptotes, holes, and intercepts. Solve rational equalities. 	Illustrative Math: Graphing Rational Functions Rational Functions Tasks pgs. 6, 13 & 15 Additional Resources: Graphing Stories: Graphic Representations of the Real Life Situations Polynomial and Rational Functions Videos	Explain why all of the test intervals must be in order to get an accurate graph of a rational function.



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RESOURCE TOOLKIT				
Textbook Resources Glencoe Precalculus © 2011 <u>http://connected.mcgraw-hill.com/connected/login.do</u> Sullivan Precalculus: Enhanced with Graphing Utilities, 5e © 2009.	Standards Common Core Standards - Mathematics Common Core Standards - Mathematics Appendix A The Mathematics Common Core Toolbox Common Core Lessons Tennessee Academic Standards for Mathematics	Videos <u>Khan Academy</u> <u>Lamar University Tutorial</u> <u>UCI Precalculus Instructional Videos</u> <u>Flipped Math - Precalculus</u>		
Calculator Texas Instruments Education Texas Instruments - Precalculus Activities Casio Education TI Emulator Math Nspired Desmos SEL Resources SEL Connections with Math Practices SEL Core Competencies The Collaborative for Academic, Social, and Emotional Learning (CASEL)	Interactive Manipulatives http://www.ct4me.net/math_manipulatives_2.htm Illuminations (NCTM) ACT & SAT TN ACT Information & Resources ACT College & Career Readiness Mathematics Standards ACT Academy SAT Connections SAT Practice from Khan Academy Tasks/Lessons UT Dana Center Inside Math Tasks Math Vision Project Tasks Better Lesson Edutoolbox GSE Precalculus: Unit 1 Introduction to Trigonometric Functions GSE Precalculus: Unit 2 Trigonometric Functions GSE Precalculus: Unit 4 Trigonometric Identities	Additional Sites http://functions.wolfram.com http://www.analyzemath.com/Graphing/piecewise_functions. html http://www.oupplemath.com/ http://www.onlinemathlearning.com/math-word-problems.html http://education.ti.com/calculators/downloads/US/Activities/D etail?id=9530 Better Lesson Algebra Cheat Sheet Trigonometry Cheat Sheet Online Algebra and Trigonometry Tutorial Study Tips for Math Courses		